

# Thermistor Constant Conversions - Beta to Steinhart-Hart



The non-linear resistance-temperature characteristics of negative-temperature coefficient (NTC) thermistors may be modeled to a high degree of accuracy using several modeling techniques. The most popular model is the Steinhart-Hart equation.

$$(1) \frac{1}{T} = C1 + C2*(\ln R) + C3*(\ln R)^3$$

An early equation called the “Beta” formula proved to be useful over narrow temperature ranges. This equation requires a two-point calibration but, under the best conditions, is accurate to approximately  $\pm 1^\circ\text{C}$  over the temperature range of  $0^\circ\text{C}$  to  $100^\circ\text{C}$ .

$$(2) R = R_0 * e^{\beta(1/T - 1/T_0)}$$

Where  $R_0$  and  $T_0$  are the “base” values for the thermistor. Temperature (T) is in Kelvin, and resistance (R) is in ohms.

If it is not possible to measure the temperature-resistance characteristics of a thermistor, this equation can be used to calculate the resistance-temperature characteristics. These resistance values can then be used in the Steinhart-Hart equation to calculate the C1, C2, and C3 constants.

Create a table of temperature-resistance values for a given Beta ( $\beta$ ). Table 1 (right) is for temperatures of 273.15, 298.15, and 323.15 K. The thermistor resistances in  $\Omega$  were calculated using equation (2) at each temperature. The values for  $R_0$ ,  $T_0$ , and  $\beta$  were 10440, 298.15, and 4140, respectively. Once the resistance values are calculated, the Steinhart-Hart equation (1) can be used to calculate the constants C1, C2, and C3. ILX Lightwave’s Application Note #4 offers pre-programmed methods for calculating C1, C2, and C3 based on the Steinhart-Hart equation.

Temperature (K)	$R_{\text{calc}}$ ( $\Omega$ )
273.15	37208
298.15	10440
323.15	3565

Table 1. Calculated Resistance Values

This method is not as accurate as actual resistance-temperature measurements because the resistance-temperature characteristics are calculated and based on a two-point calibration used to generate values for a three-point model. The magnitude of the error depends on the temperature range over which the resistance measurement is made versus the given  $T_0$ . The measured thermistor resistance will be less accurate for temperatures further away from  $T_0$ .